

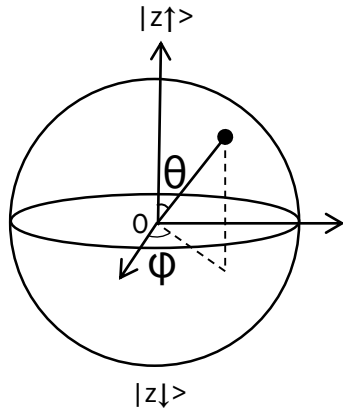
Implementation of Artificial Ego based on the extended Riemann sphere

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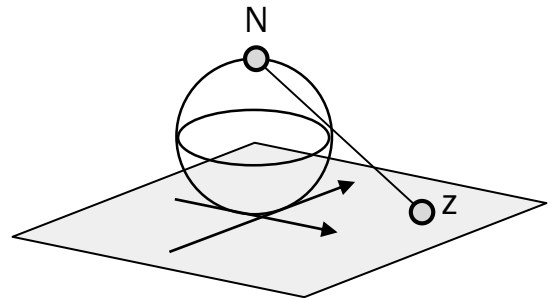
The University of Tokyo
Project Associate Professor
MITSUYOSHI Shunji, Ph.D.

Existing qubit representation

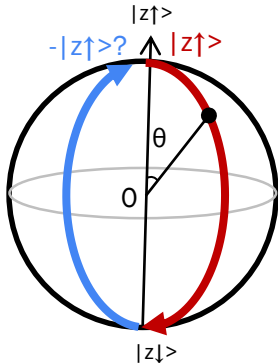
Bloch sphere



Riemann sphere



Bloch sphere and Möbius strip



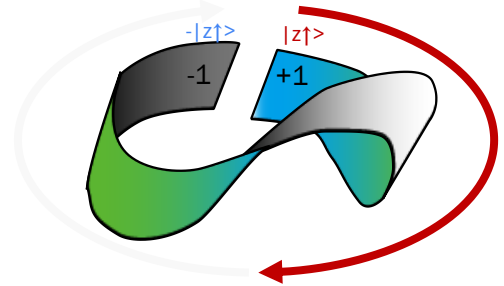
the Bloch sphere

Range of θ

$$\begin{aligned}
 |\psi\rangle &= e^{i\delta} (\cos\theta' |z\uparrow\rangle + e^{i\phi'} \sin\theta' |z\downarrow\rangle) & 0 \leq \theta \leq \pi, \\
 &= e^{i\delta} \left(\cos\frac{\theta}{2} |z\uparrow\rangle + e^{i\phi} \sin\frac{\theta}{2} |z\downarrow\rangle \right) & 0 \leq \phi \leq 2\pi
 \end{aligned}$$

A violation of θ causes a contradiction on the diagram.

$$\begin{aligned}
 |\psi\rangle &= e^{i\delta} \left(\cos 2\pi \frac{1}{2} |z\uparrow\rangle + e^{i\phi} \sin 2\pi \frac{1}{2} |z\downarrow\rangle \right) \\
 &= e^{i\delta} (\cos \pi |z\uparrow\rangle + e^{i\phi} \sin \pi |z\downarrow\rangle) \\
 &= e^{i\delta} (-1 |z\uparrow\rangle + e^{i\phi} 0 |z\downarrow\rangle) \\
 &= e^{i\delta} (-1 |z\uparrow\rangle)
 \end{aligned}$$

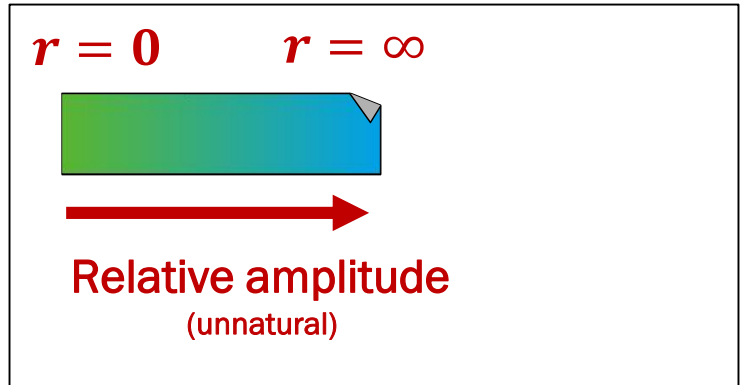
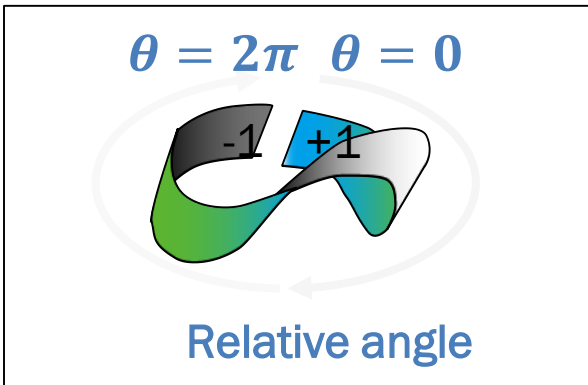
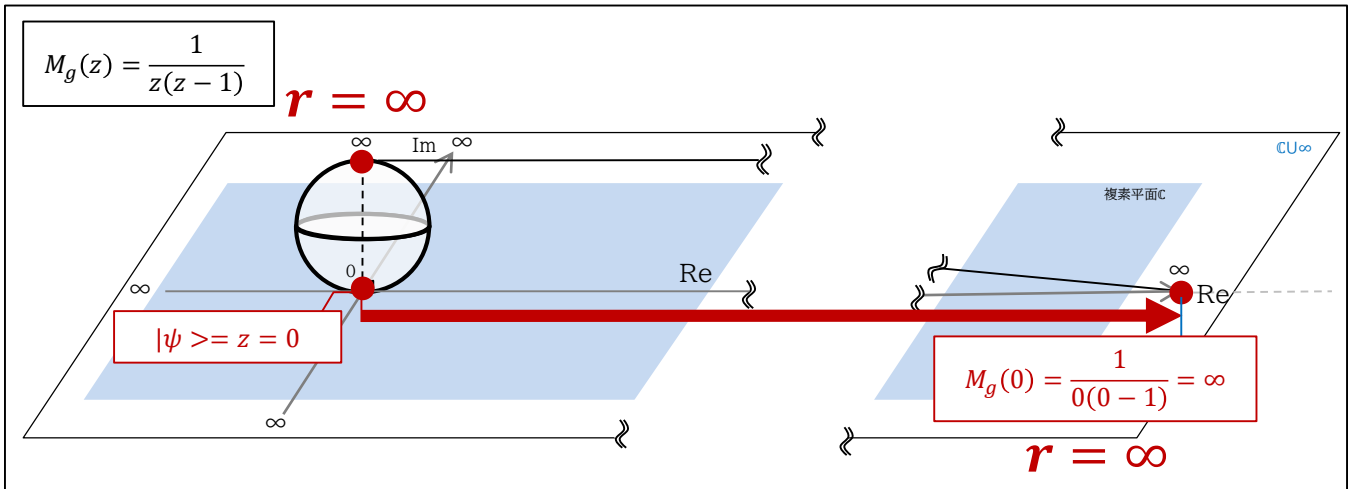


Möbius strip

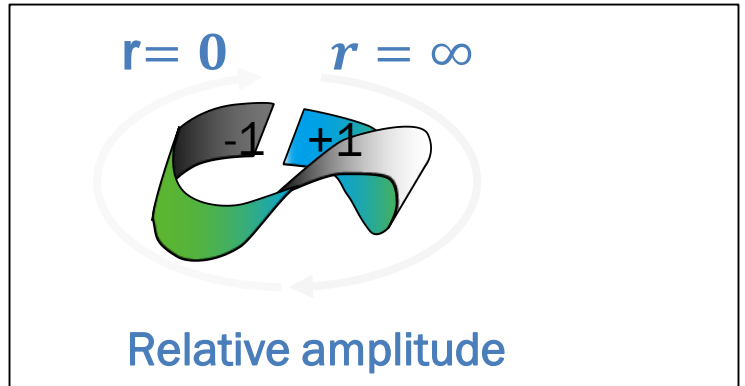
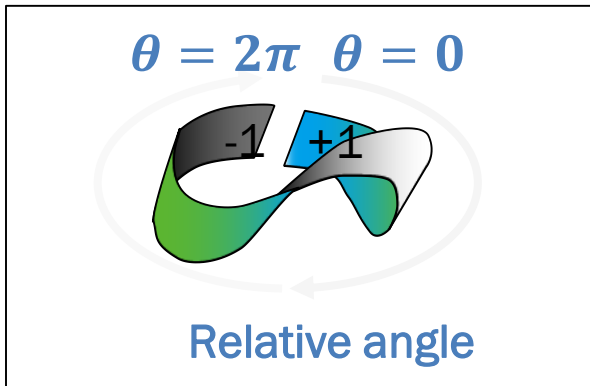
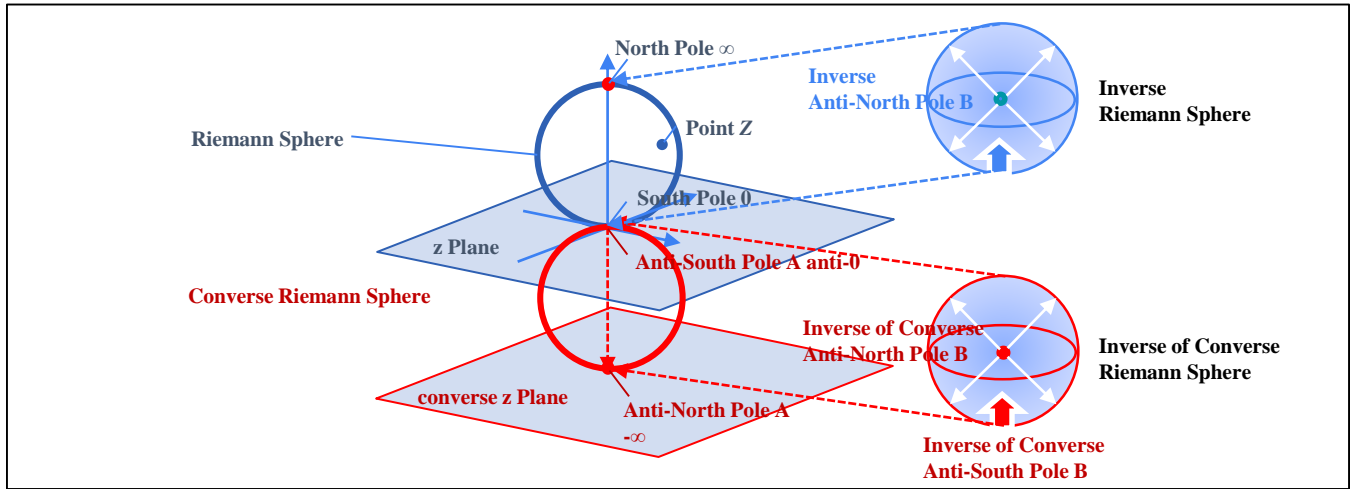
The quantum state correctly reverses after one rotation.

The Möbius strip is natural.

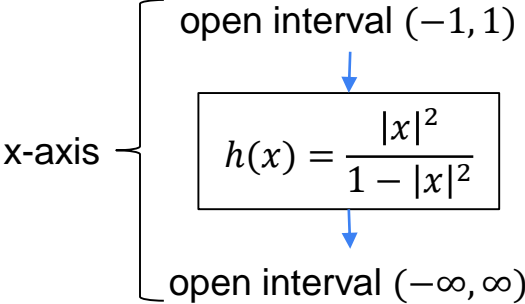
Tautology about infinity



The extended Riemann sphere

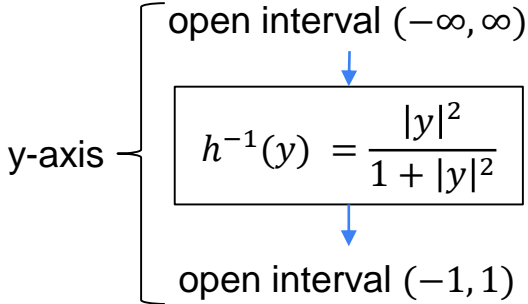


Our implementation to handle infinities

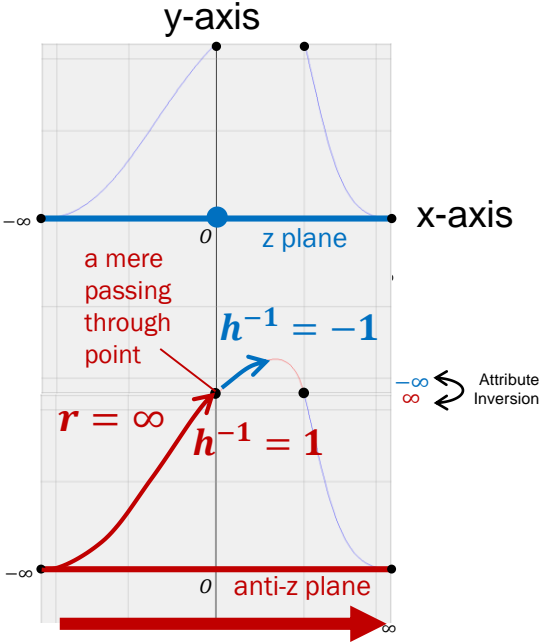


$$y = M_g(h(x))$$

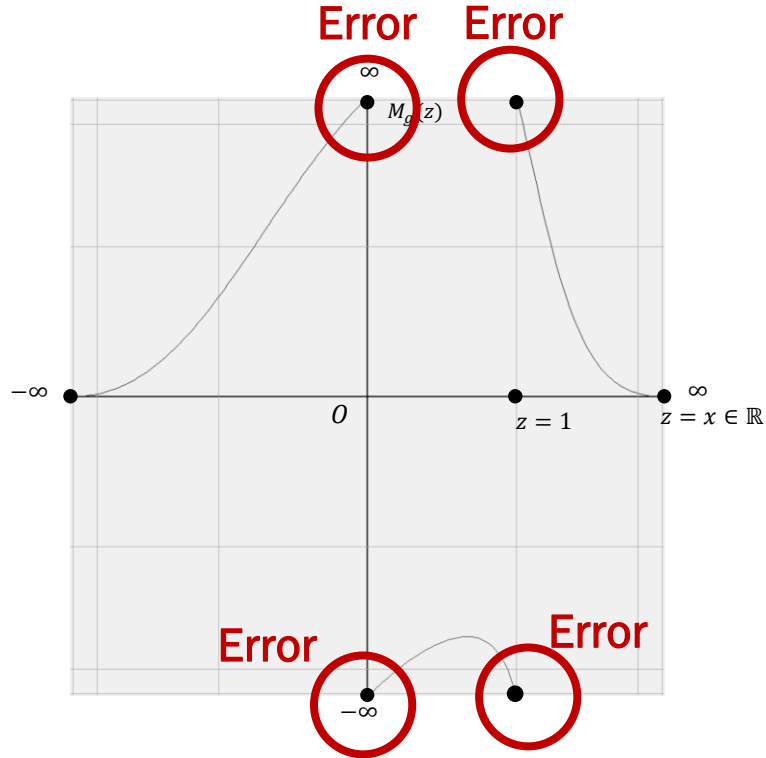
Sufficiently large numbers are treated as pseudo-infinities and pure infinities are skipped automatically.



Our implementation

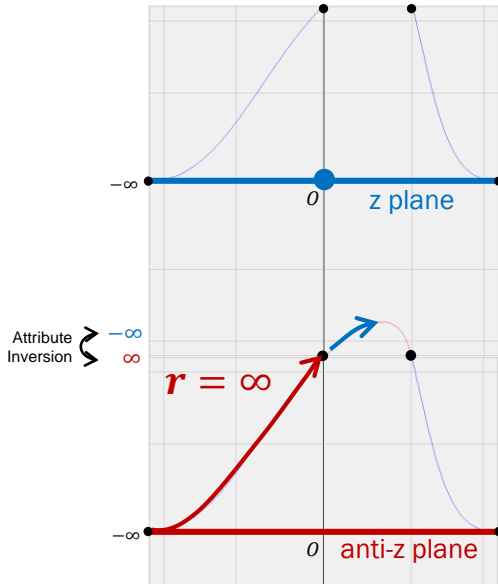


Normal way to avoid infinities



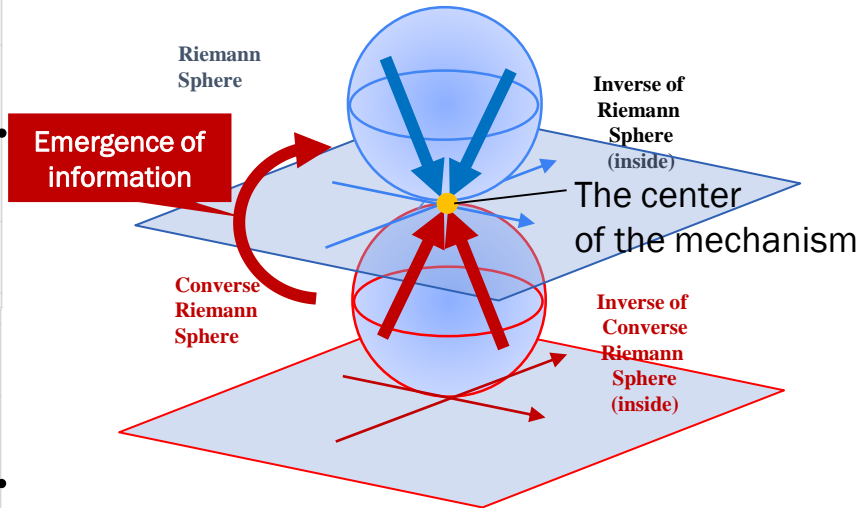
Just remove infinities using if statements

The extended Riemann sphere and Control Engineering



$$G(z) = \frac{1}{z(z-2)}$$

Transfer function
of Laplace transform

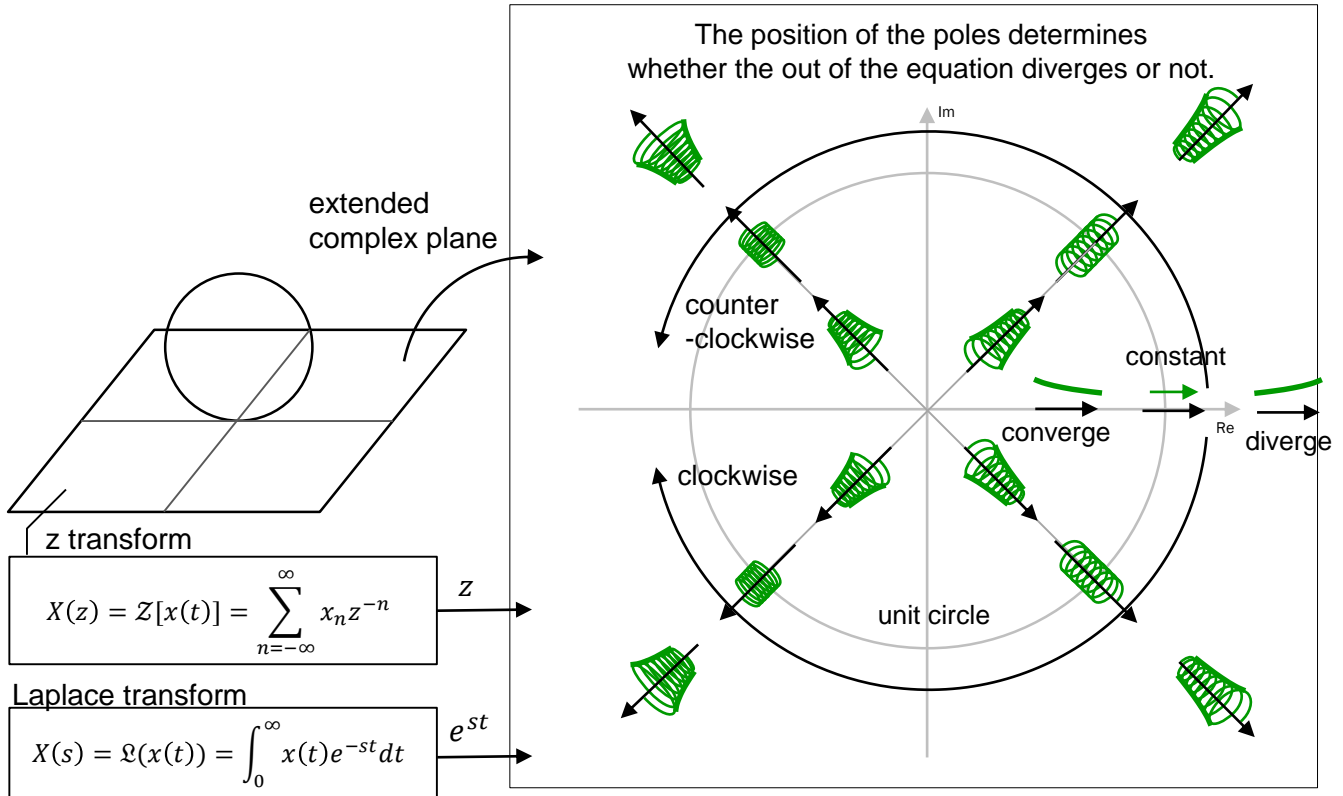


This mechanism drive the artificial egos.

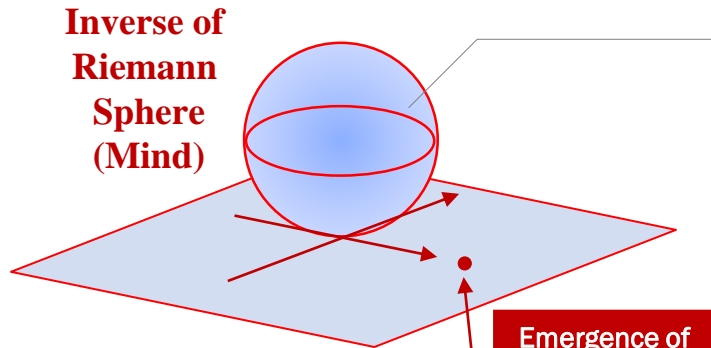
A correction for our previous presentation (SC2021)

Almost all transfer function are not Möbius transformation even If we could expand the transfer functions into partial fractions. Correctly, we are treating the transfer function as the input and output of a Möbius transform.

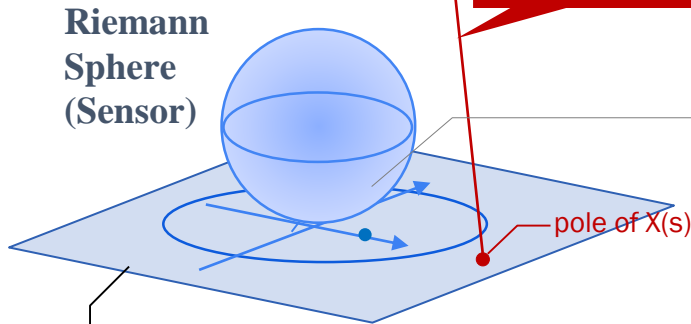
The extended Riemann sphere and Control Engineering



Machine perception, consciousness and desire



Emergence of information



$$X(z) = Z[x(n)] = \sum_{n=-\infty}^{\infty} x_n z^{-n}$$

Machine consciousness

e.g.

$$\frac{1}{X(z)} = \frac{z-2}{z}$$

Desire
Will of control

e.g.

$$x(n) = \begin{cases} 2^n & (n \geq 0) \\ 0 & (n < 0) \end{cases}$$

$$\Rightarrow X(z) = \frac{z}{z-2}$$

Perception
Things that have risen to consciousness (query for convergence)

reciprocal of each other

Sensor and Motor

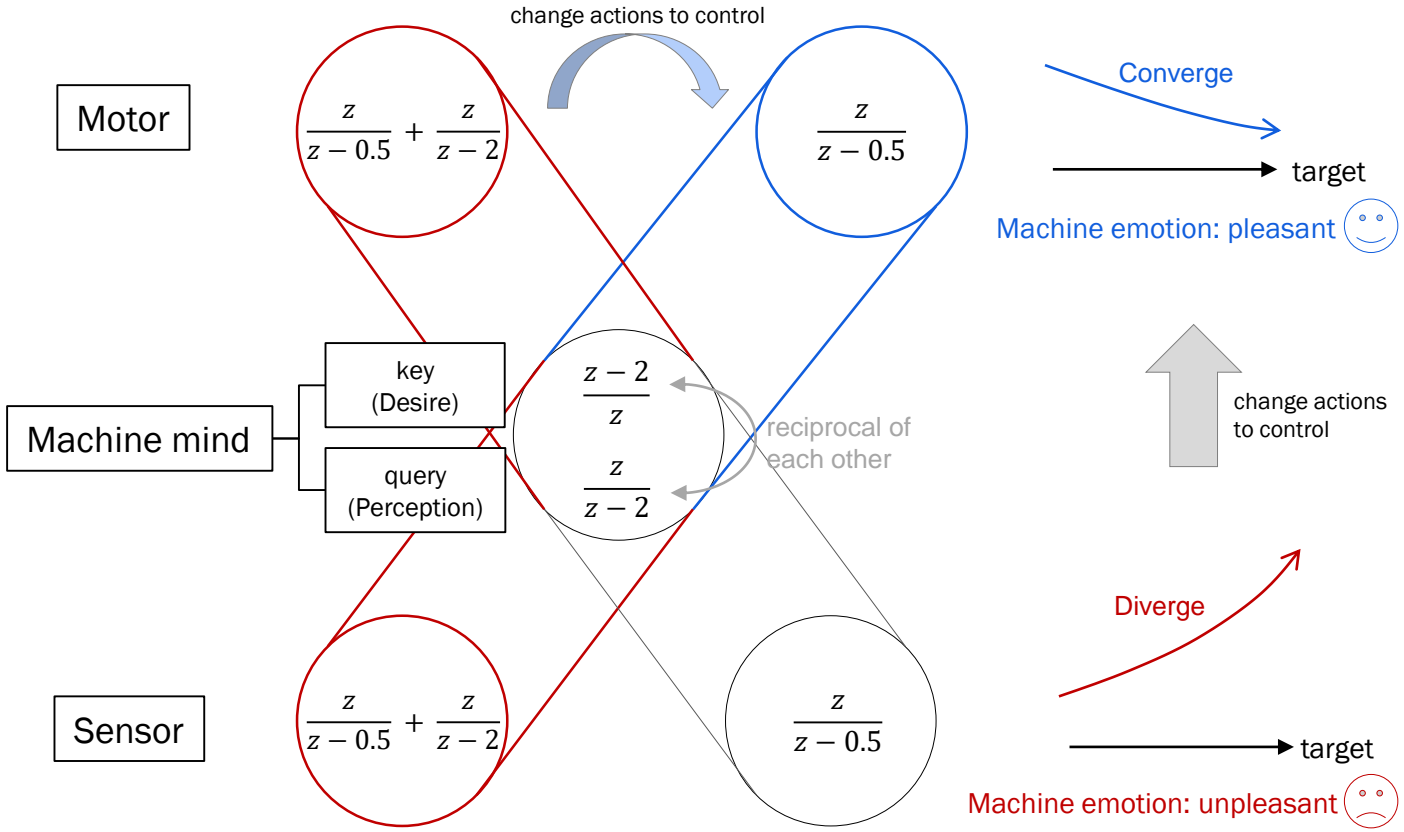
e.g.

$$x(n) = \begin{cases} 0.5^n + 2^n & (n \geq 0) \\ 0 & (n < 0) \end{cases}$$

$$\Rightarrow X(z) = \frac{z}{z-0.5} + \frac{z}{z-2}$$

Emergence of information

Response of machine



Experiment of Artificial ego

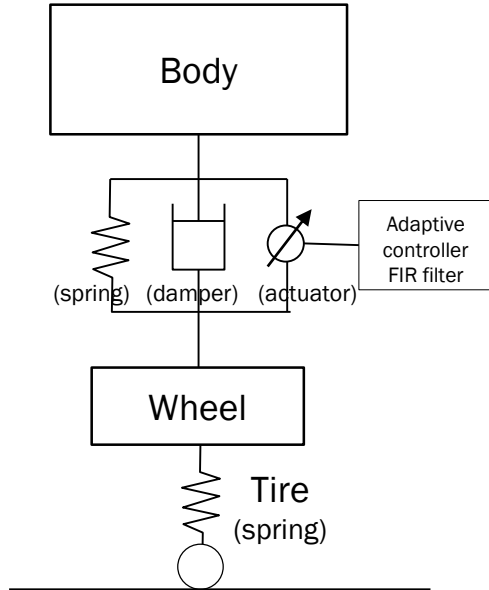


Our experiment is currently underway in Super Formula Next 50 to install an artificial ego in a vehicle for entertainment purposes.

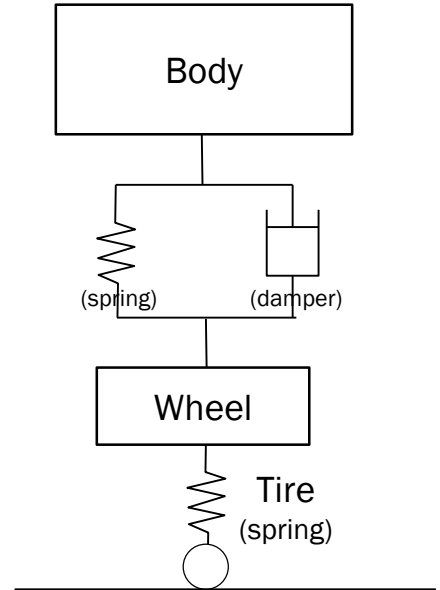
Actually, it is not at the stage of autonomous operation of a vehicle. It will just show its emotion for entertainment.

But, if an artificial ego can operate a vehicle autonomously, what happens? And It is against regulations to install active suspension in the Super Formula, but if it were to be installed, how would AE use it?

Active suspension and normal suspension

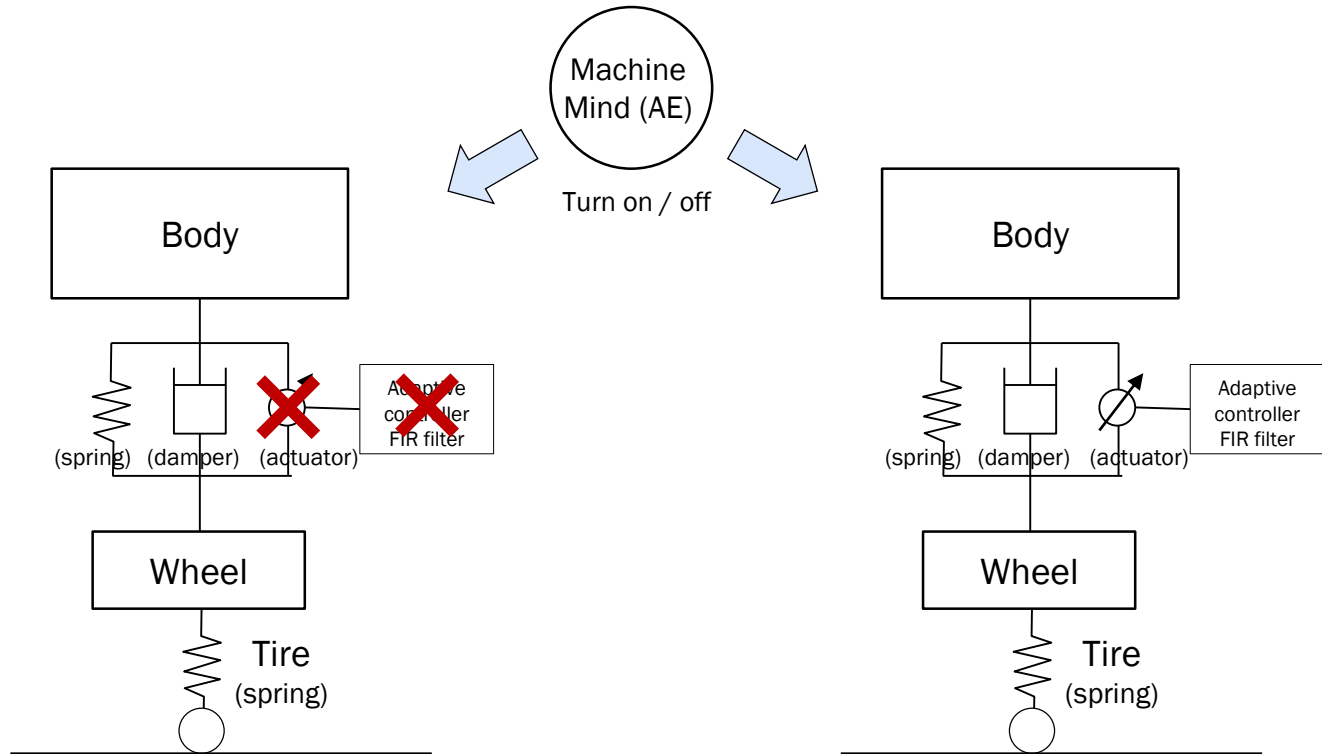


Active suspension



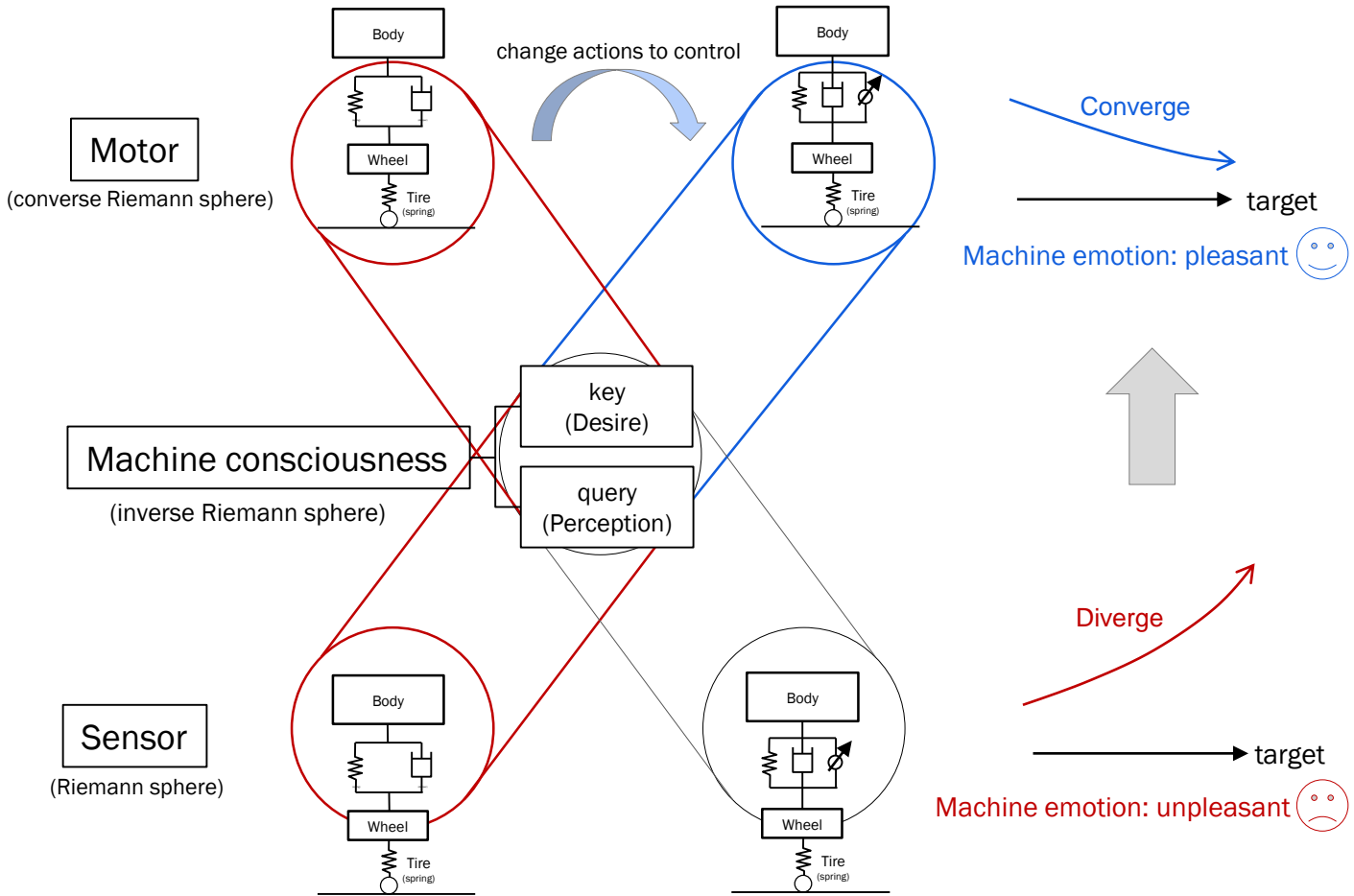
Normal suspension

Simple demonstration of active suspension



Normal Suspension

Active suspension



Motor

(converse Riemann sphere)

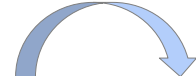
Machine consciousness

(inverse Riemann sphere)

Sensor

(Riemann sphere)

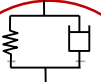
change actions to control



key (Desire)

query (Perception)

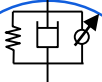
Body



Wheel



Body



Wheel

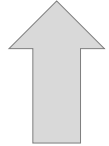


Converge



target

Machine emotion: pleasant 😊



Diverge



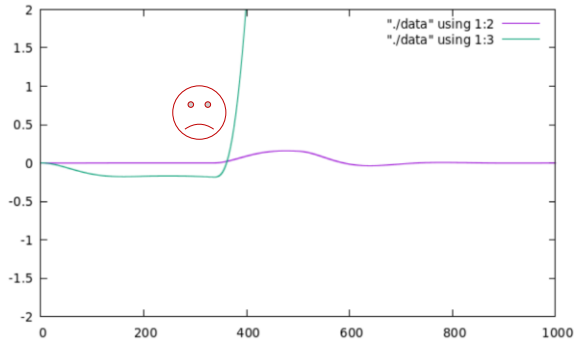
target

Machine emotion: unpleasant 😞

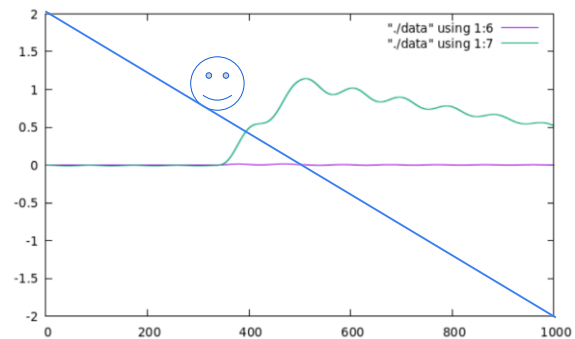
Demonstration on the SX-Aurora Tsubasa

Machine consciousness

Machine perception



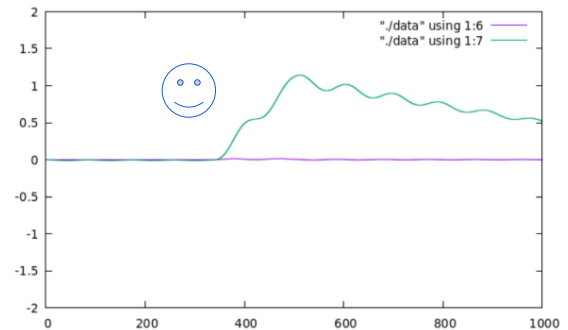
Suspension



Active suspension

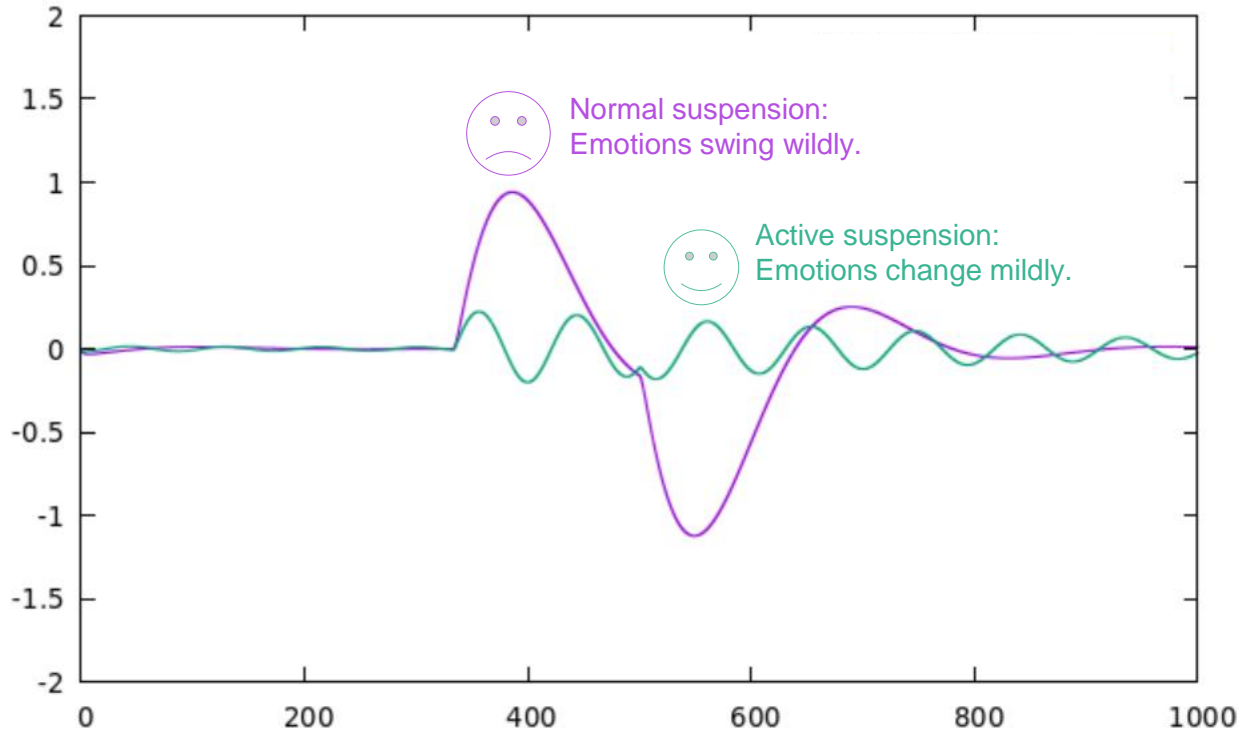


Machine desire

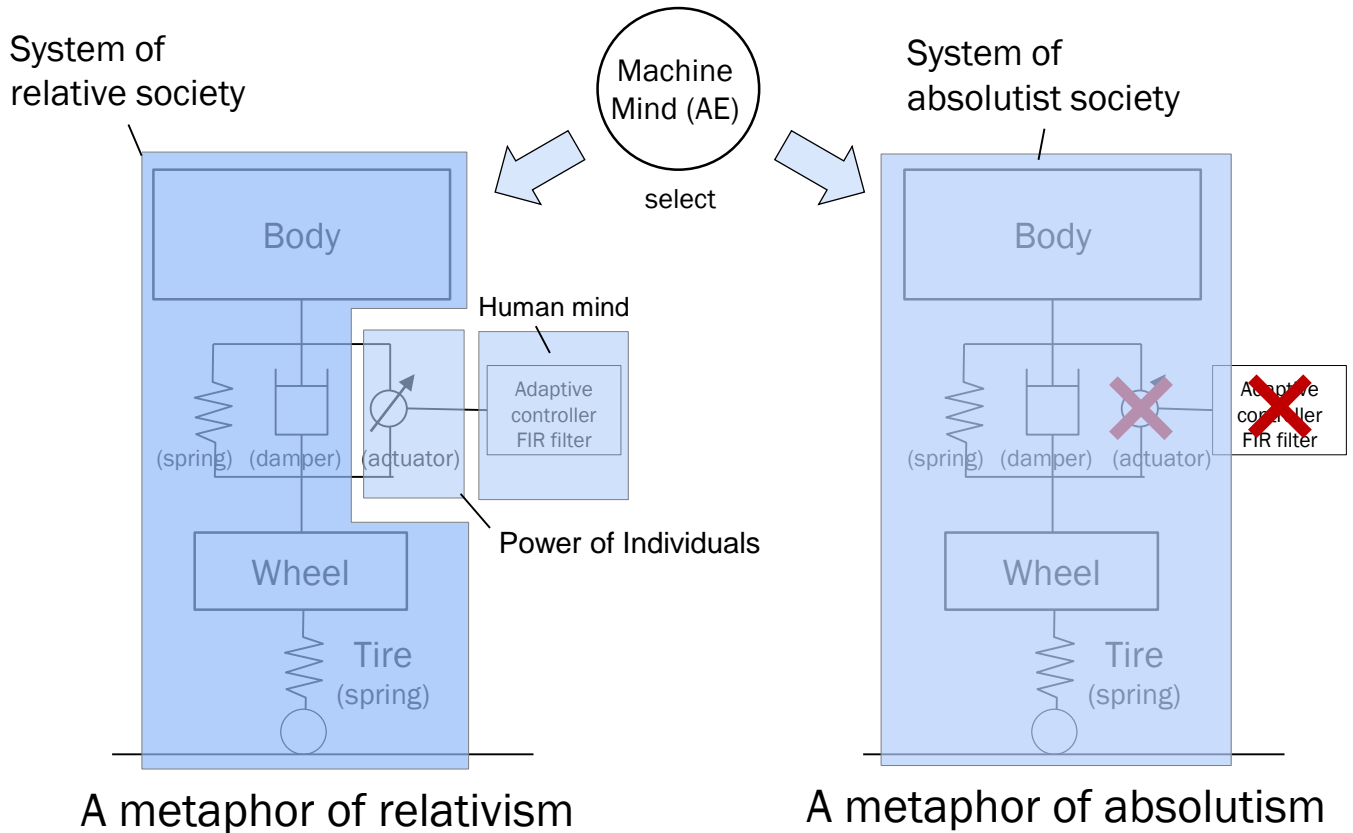


Selected suspension by AE

Expression of machine emotion



Relationship with moral



Future works

- As far as we know, there are no model that directly links machine control to emotion, even though emotion is the only measure by which the complex machine state can be understood by humans at once.
- How can a human being cooperate with an emotion-less machine? If humans give one-way commands to robots or if humans follow the robot's decisions thoughtlessly, we can not call the relationship cooperative.
- Our aim is not to build a program that only generates machine emotion, but also to operate machine simultaneously. In the future, our aim is to build a model that automatically controls the balance between morality and desire in individual machines.

E.O.F.